

Production and Cost Relationships Review

Production function:

$Q = f(L, K, R, \text{technology, cultural and legal, } \dots)$

Long run: $Q = f(L, K, R)$, *ceteris paribus*

Short run: $Q = f(L)$ *ceteris paribus* (L is the variable input in this example, K and/or R are the fixed inputs "Scale of Plant")

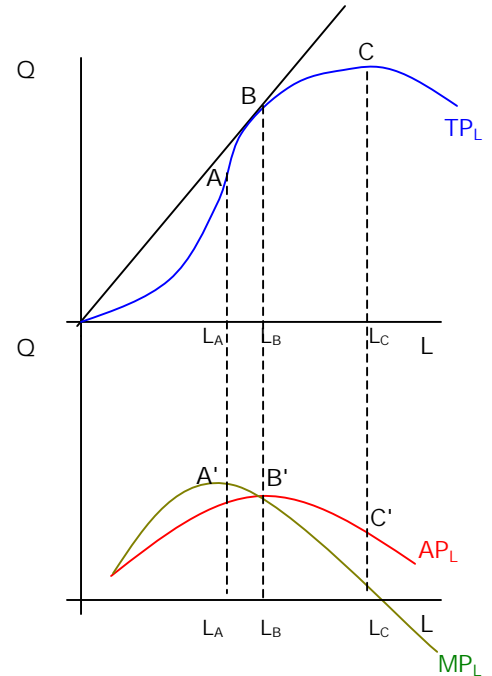
$Q = TP_L = f(\text{inputs, technology, etc})$

$$AP_L = \frac{TP_L}{L} = \frac{Q}{L}$$

$$MP_L = \frac{\Delta TP}{\Delta L} = \frac{\Delta Q}{\Delta L}$$

$$MP_L = \frac{\partial Q}{\partial L}, \quad MP_K = \frac{\partial Q}{\partial K}, \quad MP_R = \frac{\partial Q}{\partial R}$$

- Inflection point is at L_A (point A), maximum of MP_L at L_A (point A')
- At L_B , tan of ray from origin at point B, maximum of AP_L at B'
- At L_C , TP_L is a maximum, $MP_L = 0$
- When $AP_L = MP_L$, AP_L is a maximum, when $MP > AP$, AP rises, $MP < AP$, AP decreases



Cost Functions:

Short run

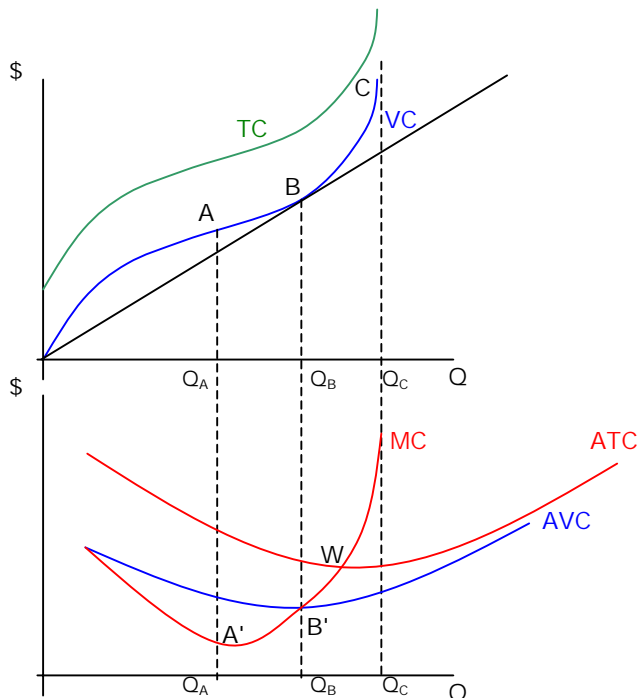
$FC = TFC = (P_K) * K$, where K is fixed input

$FC = TC - VC$

$VC = TFC = (P_L) * L$, where L is variable input

$VC = TC - FC$

$TC = VC + FC$



$$AVC = \frac{VC}{Q} = ATC - AFC$$

$$AVC = \left(\frac{1}{AP_L}\right) * P_L$$

$$AFC = \frac{FC}{Q} = ATC - AVC$$

$$ATC = \frac{TC}{Q} = AVC + AFC$$

$$MC = \frac{\Delta TC}{\Delta Q} = \frac{\Delta VC}{\Delta Q}$$

$$MC = \left(\frac{1}{MP_L}\right) * P_L$$

- At inflection point A (at Q_A), MC is a minimum, MP_L is a maximum
- At output Q_B (point B) AVC is a minimum
- When $MC < AVC$, AVC is falling
- When $MC > AVC$, AVC is rising
- When $MC = AVC$, AVC is a min.
- When AVC is a min, AP_L is a max.
- When $MC < ATC$, ATC is falling
- When $MC > ATC$, ATC is rising
- When $MC = ATC$, ATC is a min.
- When AVC is a min, AP_L is a max
- When MC is a min, MP_L is a max
- The vertical distance between AVC and ATC is the AFC